

Day 1
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Course Outline: Algebra 2

Class is from 8:30-10:00 on Tuesdays and Thursdays

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This class is designed to help you learn many of the algebra concepts that are necessary to know, in order to pass the math section of the HiSet.

<https://www.youtube.com/watch?v=KBpNLjiv8pk>

Week	Dates	Main Topics to be covered
Week 1	January 21	Intro. to variables and reading equations as sentences
Week 2	January 27- 29	Exponents and order of operations
Week 3	February 3-5	Important terms and working with formulas
Week 4	February 10-12	Distributive property
Mardi Gras	February 17-19	No Class
Week 5	February 24-26	Solving equations
Week 6	March 3-5	Writing equations from word problems
Week 7	March 10-12	Inequities
Week 8	March 17-20	Review

Solving Linear Equations - One Step Equations

Objective: Solve one step linear equations by balancing using inverse operations

Solving linear equations is an important and fundamental skill in algebra. In algebra, we are often presented with a problem where the answer is known, but part of the problem is missing. The missing part of the problem is what we seek to find. An example of such a problem is shown below.

Example 41.

$$4x + 16 = -4$$

Notice the above problem has a missing part, or unknown, that is marked by x . If we are given that the solution to this equation is -5 , it could be plugged into the equation, replacing the x with -5 . This is shown in Example 2.

Example 42.

$$\begin{aligned} 4(-5) + 16 &= -4 && \text{Multiply } 4(-5) \\ -20 + 16 &= -4 && \text{Add } -20 + 16 \\ -4 &= -4 && \text{True!} \end{aligned}$$

Now the equation comes out to a true statement! Notice also that if another number, for example, 3, was plugged in, we would not get a true statement as seen in Example 3.

Example 43.

$$\begin{aligned} 4(3) + 16 &= -4 && \text{Multiply } 4(3) \\ 12 + 16 &= -4 && \text{Add } 12 + 16 \\ 28 &\neq -4 && \text{False!} \end{aligned}$$

Due to the fact that this is not a true statement, this demonstrates that 3 is not the solution. However, depending on the complexity of the problem, this “guess and check” method is not very efficient. Thus, we take a more algebraic approach to solving equations. Here we will focus on what are called “one-step equations” or equations that only require one step to solve. While these equations often seem very fundamental, it is important to master the pattern for solving these problems so we can solve more complex problems.



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Addition Problems

To solve equations, the general rule is to do the opposite. For example, consider the following example.

Example 44.

$$\begin{array}{ll} x + 7 = -5 & \text{The 7 is added to the } x \\ \underline{-7 \quad -7} & \text{Subtract 7 from both sides to get rid of it} \\ x = -12 & \text{Our solution!} \end{array}$$

Then we get our solution, $x = -12$. The same process is used in each of the following examples.

Example 45.

$$\begin{array}{r} 4 + x = 8 \\ \underline{-4 \quad -4} \\ x = 4 \end{array}$$

$$\begin{array}{r} 7 = x + 9 \\ \underline{-9 \quad -9} \\ -2 = x \end{array}$$

$$\begin{array}{r} 5 = 8 + x \\ \underline{-8 \quad -8} \\ -3 = x \end{array}$$

Table 1. Addition Examples

Subtraction Problems

In a subtraction problem, we get rid of negative numbers by adding them to both sides of the equation. For example, consider the following example.

Example 46.

$$\begin{array}{ll} x - 5 = 4 & \text{The 5 is negative, or subtracted from } x \\ \underline{+5 \quad +5} & \text{Add 5 to both sides} \\ x = 9 & \text{Our Solution!} \end{array}$$

Then we get our solution $x = 9$. The same process is used in each of the following examples. Notice that each time we are getting rid of a negative number by adding.



Example 47.

$$\begin{array}{r} -6 + x = -2 \\ +6 \quad +6 \\ \hline x = 4 \end{array}$$

$$\begin{array}{r} -10 = x - 7 \\ +7 \quad +7 \\ \hline -3 = x \end{array}$$

$$\begin{array}{r} 5 = -8 + x \\ +8 \quad +8 \\ \hline 13 = x \end{array}$$

Table 2. Subtraction Examples

Multiplication Problems

With a multiplication problem, we get rid of the number by dividing on both sides. For example consider the following example.

Example 48.

$$\begin{array}{r} 4x = 20 \\ \hline 4 \quad 4 \\ \hline x = 5 \end{array}$$

Variable is multiplied by 4
Divide both sides by 4
Our solution!

Then we get our solution $x = 5$

With multiplication problems it is very important that care is taken with signs. If x is multiplied by a negative then we will divide by a negative. This is shown in example 9.

Example 49.

$$\begin{array}{r} -5x = 30 \\ \hline -5 \quad -5 \\ \hline x = -6 \end{array}$$

Variable is multiplied by -5
Divide both sides by -5
Our Solution!

The same process is used in each of the following examples. Notice how negative and positive numbers are handled as each problem is solved.

Example 50.



$$\begin{array}{r} 8x = -24 \\ \hline 8 \quad \hline 8 \\ x = -3 \end{array}$$

$$\begin{array}{r} -4x = -20 \\ \hline -4 \quad \hline -4 \\ x = 5 \end{array}$$

$$\begin{array}{r} 42 = 7x \\ \hline 7 \quad \hline 7 \\ 6 = x \end{array}$$

Table 3. Multiplication Examples

Division Problems:

In division problems, we get rid of the denominator by multiplying on both sides. For example consider our next example.

Example 51.

$$\begin{array}{ll} \frac{x}{5} = -3 & \text{Variable is divided by 5} \\ (5)\frac{x}{5} = -3(5) & \text{Multiply both sides by 5} \\ x = -15 & \text{Our Solution!} \end{array}$$

Then we get our solution $x = -15$. The same process is used in each of the following examples.

Example 52.

$$\begin{array}{r} \frac{x}{-7} = -2 \\ (-7)\frac{x}{-7} = -2(-7) \\ x = 14 \end{array}$$

$$\begin{array}{r} \frac{x}{8} = 5 \\ (8)\frac{x}{8} = 5(8) \\ x = 40 \end{array}$$

$$\begin{array}{r} \frac{x}{-4} = 9 \\ (-4)\frac{x}{-4} = 9(-4) \\ x = -36 \end{array}$$

Table 4. Division Examples

The process described above is fundamental to solving equations. once this process is mastered, the problems we will see have several more steps. These problems may seem more complex, but the process and patterns used will remain the same.

World View Note: The study of algebra originally was called the “Cossic Art” from the Latin, the study of “things” (which we now call variables).



1.1 Practice - One Step Equations

Solve each equation.

1/22

1) $v + 9 = 16$

2) $14 = b + 3$

3) $x - 11 = -16$

4) $-14 = x - 18$

5) $30 = a + 20$

6) $-1 + k = 5$

7) $x - 7 = -26$

8) $-13 + p = -19$

9) $13 = n - 5$

10) $22 = 16 + m$

11) $340 = -17x$

12) $4r = -28$

13) $-9 = \frac{n}{12}$

14) $\frac{5}{9} = \frac{b}{9}$

15) $20v = -160$

16) $-20x = -80$

17) $340 = 20n$

18) $\frac{1}{2} = \frac{a}{8}$

19) $16x = 320$

20) $\frac{k}{13} = -16$

21) $-16 + n = -13$

22) $21 = x + 5$

23) $p - 8 = -21$

24) $m - 4 = -13$

25) $180 = 12x$

26) $3n = 24$

27) $20b = -200$

28) $-17 = \frac{x}{12}$

29) $\frac{r}{14} = \frac{5}{14}$

30) $n + 8 = 10$

31) $-7 = a + 4$

32) $v - 16 = -30$

33) $10 = x - 4$

34) $-15 = x - 16$

35) $13a = -143$

36) $-8k = 120$

37) $\frac{p}{20} = -12$

38) $-15 = \frac{x}{9}$

39) $9 + m = -7$

40) $-19 = \frac{n}{20}$

Finish
for
HW

